

1. Let  $\mathbf{X} = \begin{pmatrix} x \\ y \end{pmatrix}$ . Then  $\mathbf{X}' = \begin{pmatrix} 3 & -5 \\ 4 & 8 \end{pmatrix} \mathbf{X}$ .

3. Let  $\mathbf{X} = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$ . Then  $\mathbf{X}' = \begin{pmatrix} -3 & 4 & -9 \\ 6 & -1 & 0 \\ 10 & 4 & 3 \end{pmatrix} \mathbf{X}$ .

9.  $\frac{dx}{dt} = x - y + 2z + e^{-t} - 3t$ ;  $\frac{dy}{dt} = 3x - 4y + z + 2e^{-t} + t$ ;  $\frac{dz}{dt} = -2x + 5y + 6z + 2e^{-t} - t$

11. Since

$$\mathbf{X}' = \begin{pmatrix} -5 \\ -10 \end{pmatrix} e^{-5t} \quad \text{and} \quad \begin{pmatrix} 3 & -4 \\ 4 & -7 \end{pmatrix} \mathbf{X} = \begin{pmatrix} -5 \\ -10 \end{pmatrix} e^{-5t}$$

we see that

$$\mathbf{X}' = \begin{pmatrix} 3 & -4 \\ 4 & -7 \end{pmatrix} \mathbf{X}.$$

17. Yes, since  $W(\mathbf{X}_1, \mathbf{X}_2) = -2e^{-8t} \neq 0$  the set  $\mathbf{X}_1, \mathbf{X}_2$  is linearly independent on  $-\infty < t < \infty$ .

21. Since

$$\mathbf{X}'_p = \begin{pmatrix} 2 \\ -1 \end{pmatrix} \quad \text{and} \quad \begin{pmatrix} 1 & 4 \\ 3 & 2 \end{pmatrix} \mathbf{X}_p + \begin{pmatrix} 2 \\ -4 \end{pmatrix} t + \begin{pmatrix} -7 \\ -18 \end{pmatrix} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

we see that

$$\mathbf{X}'_p = \begin{pmatrix} 1 & 4 \\ 3 & 2 \end{pmatrix} \mathbf{X}_p + \begin{pmatrix} 2 \\ -4 \end{pmatrix} t + \begin{pmatrix} -7 \\ -18 \end{pmatrix}.$$