

$$\begin{aligned} 1. \quad \mathcal{L}\{f(t)\} &= \int_0^1 -e^{-st} dt + \int_1^\infty e^{-st} dt = \frac{1}{s} e^{-st} \Big|_0^1 - \frac{1}{s} e^{-st} \Big|_1^\infty \\ &= \frac{1}{s} e^{-s} - \frac{1}{s} - \left(0 - \frac{1}{s} e^{-s}\right) = \frac{2}{s} e^{-s} - \frac{1}{s}, \quad s > 0 \end{aligned}$$

$$\begin{aligned} 3. \quad \mathcal{L}\{f(t)\} &= \int_0^1 t e^{-st} dt + \int_1^\infty e^{-st} dt = \left(-\frac{1}{s} t e^{-st} - \frac{1}{s^2} e^{-st}\right) \Big|_0^1 - \frac{1}{s} e^{-st} \Big|_1^\infty \\ &= \left(-\frac{1}{s} e^{-s} - \frac{1}{s^2} e^{-s}\right) - \left(0 - \frac{1}{s^2}\right) - \frac{1}{s}(0 - e^{-s}) = \frac{1}{s^2}(1 - e^{-s}), \quad s > 0 \end{aligned}$$

9. The function is $f(t) = \begin{cases} 1-t, & 0 < t < 1 \\ 0, & t > 1 \end{cases}$ so

$$\begin{aligned} \mathcal{L}\{f(t)\} &= \int_0^1 (1-t) e^{-st} dt + \int_1^\infty 0 e^{-st} dt = \int_0^1 (1-t) e^{-st} dt = \left(-\frac{1}{s}(1-t) e^{-st} + \frac{1}{s^2} e^{-st}\right) \Big|_0^1 \\ &= \frac{1}{s^2} e^{-s} + \frac{1}{s} - \frac{1}{s^2}, \quad s > 0 \end{aligned}$$