

3. Let  $b$  be the rate of births and  $d$  the rate of deaths. Then  $b = k_1P$  and  $d = k_2P^2$ . Since  $dP/dt = b - d$ , the differential equation is  $dP/dt = k_1P - k_2P^2$ .

5. From the graph in the text we estimate  $T_0 = 180^\circ$  and  $T_m = 75^\circ$ . We observe that when  $T = 85$ ,  $dT/dt \approx -1$ . From the differential equation we then have

$$k = \frac{dT/dt}{T - T_m} = \frac{-1}{85 - 75} = -0.1.$$

7. The number of students with the flu is  $x$  and the number not infected is  $1000 - x$ , so  $dx/dt = kx(1000 - x)$ .

9. The rate at which salt is leaving the tank is

$$R_{out} (3 \text{ gal/min}) \cdot \left(\frac{A}{300} \text{ lb/gal}\right) = \frac{A}{100} \text{ lb/min.}$$

Thus  $dA/dt = -A/100$  (where the minus sign is used since the amount of salt is decreasing. The initial amount is  $A(0) = 50$ ).

15. Since  $i = dq/dt$  and  $Ld^2q/dt^2 + Rdq/dt = E(t)$ , we obtain  $Ldi/dt + Ri = E(t)$ .