Solution Set 1.1

- 1. Second order; linear
- 3. Fourth order; linear
- 5. Second order; nonlinear because of $(dy/dx)^2$ or $\sqrt{1+(dy/dx)^2}$
- 7. Third order; linear
- 11. From $y = e^{-x/2}$ we obtain $y' = -\frac{1}{2}e^{-x/2}$. Then $2y' + y = -e^{-x/2} + e^{-x/2} = 0$.
- 13. From $y = e^{3x} \cos 2x$ we obtain $y' = 3e^{3x} \cos 2x 2e^{3x} \sin 2x$ and $y'' = 5e^{3x} \cos 2x 12e^{3x} \sin 2x$, so that y'' 6y' + 13y = 0.
- 27. From $y = e^{mx}$ we obtain $y' = me^{mx}$. Then y' + 2y = 0 implies

$$me^{mx} + 2e^{mx} = (m+2)e^{mx} = 0.$$

Since $e^{mx} > 0$ for all x, m = -2. Thus $y = e^{-2x}$ is a solution.

29. From $y = e^{mx}$ we obtain $y' = me^{mx}$ and $y'' = m^2 e^{mx}$. Then y'' - 5y' + 6y = 0 implies

$$m^2e^{mx} - 5me^{mx} + 6e^{mx} = (m-2)(m-3)e^{mx} = 0.$$

Since $e^{mx} > 0$ for all x, m = 2 and m = 3. Thus $y = e^{2x}$ and $y = e^{3x}$ are solutions.

In Problems 33-36 we substitute y = c into the differential equations and use y' = 0 and y'' = 0

33. Solving 5c = 10 we see that y = 2 is a constant solution.