

## Homework 12

1. Let  $X$  be the figure-eight graph and  $Y$  the theta graph. Describe maps  $f: X \rightarrow Y$  and  $g: Y \rightarrow X$  that are homotopy inverses.
2. Construct an explicit deformation retraction from  $\mathbb{R}^n - \{\mathbf{0}\}$  to  $S^{n-1}$ .
3. Show that the retract of a contractible space is contractible.
4. Construct a 2–dimensional cell complex that contains both an annulus  $S^1 \times I$  and a Möbius band as deformation retracts.
5. Show that  $S^\infty$  is contractible.